# Effects of molecular and particle scatterings on the model parameter for remote-sensing reflectance

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For optically deep waters, remote-sensing reflectance  $(r_{\rm rs})$  is traditionally expressed as the ratio of the backscattering coefficient  $(b_b)$  to the sum of absorption and backscattering coefficients  $(a + b_b)$  that multiples a model parameter (g, or the so-called f'/Q). Parameter g is further expressed as a function of  $b_b/(a + b_b)$  (or  $b_b/a$ ) to account for its variation that is due to multiple scattering. With such an approach, the same g value will be derived for different a and  $b_b$  values that provide the same ratio. Because g is partially a measure of the angular distribution of upwelling light, and the angular distribution from molecular scattering is quite different from that of particle scattering; g values are expected to vary with different scattering distributions even if the  $b_b/a$  ratios are the same. In this study, after numerically demonstrating the effects of molecular and particle scatterings on the values of g, an innovative  $r_{\rm rs}$  model is developed. This new model expresses  $r_{\rm rs}$  in two separate terms: one governed by the phase function of molecular scattering and one governed by the phase function of particle scattering, with a model parameter introduced for each term. In this way the phase function effects from molecular and particle scatterings are explicitly separated and accounted for. This new model provides an analytical tool to understand and quantify the phase-function effects on  $r_{rs}$ , and a platform to calculate  $r_{\rm rs}$  spectrum quickly and accurately that is required for remote-sensing applications. © 2004 Optical Society of America

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#### 1. Introduction

Ocean color can be measured by subsurface remotesensing reflectance  $(r_{\rm rs})$ ,<sup>1–3</sup> which is defined as a ratio of upwelling radiance  $[L_u(0-)]$  to downwelling irradiance  $[E_d(0-)]$  at zero depth:

$$r_{\rm rs} = \frac{L_u(0-)}{E_d(0-)}.$$
 (1)

Since  $r_{\rm rs}$  can be evaluated remotely,<sup>4</sup> the relationship between  $r_{\rm rs}$  and in-water constituents provides the bridge to estimate water properties analytically from remotely sensed data.

This  $r_{\rm rs}$  versus water property relationship can be inexplicitly evaluated by numerical tools such as the

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Monte Carlo method<sup>5,6</sup> or the HydroLight model.<sup>7</sup> Numerical simulation itself, however, cannot describe explicitly the dependences of ocean color on water property, and the intensive computation limits its feasibility to process global images in satellite remote sensing. To understand the factors that influence ocean color<sup>1,2,8,9</sup> and to implement ocean color algorithms that are based on analytical or semianalytical models,<sup>10–12</sup> a basic requirement is to have an accurate and theoretically based analytical model to link ocean color with water's inherent optical properties.<sup>13,14</sup> Earlier studies<sup>6,15</sup> found some limitations of existing models for remote-sensing reflectance. In this study, we present an improved semianalytical model to describe this relationship.

Through theoretical analyses and numerical modeling,<sup>1–3,6,16</sup>  $r_{\rm rs}$  is found generally proportional to the ratio of  $b_b/(a + b_b)$ . Here *a* is the absorption coefficient and  $b_b$  is the backscattering coefficient of bulk water.<sup>17,18</sup> In remote-sensing applications that require a forward model to calculate  $r_{\rm rs}$ ,<sup>11,12,19,20</sup> the most widely used relationship is the model reported by Gordon *et al.*<sup>5</sup>:

$$r_{\rm rs} = g \, \frac{b_b}{a + b_b},\tag{2}$$

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$$g = g_0 + g_1 \frac{b_b}{a + b_b},\tag{3}$$

and  $g_0 = 0.0949$  and  $g_1 = 0.0794$  for nadir-viewed  $r_{rs}$ .

There are two limitations for use of the combination of Eqs. (2) and (3) to model  $r_{\rm rs}.$   $\_$  First, only nadir  $g_0$  and  $g_1$  values were provided by Gordon *et al.*,<sup>5</sup> but many sensors measure water color away from nadir to avoid sunglint,<sup>21</sup> and it is known that the angular distribution of  $r_{\rm rs}$  is not isotropic.<sup>22,23</sup> Uncertainties arise when using nadir-viewed r<sub>rs</sub> models to interpret  $r_{\rm rs}$  values measured at other angles. Second, Eq. (3) will give the same g value for different a and  $b_b$  values as long as they result in the same  $b_b/(a + b_b)$  ratio. Note that  $r_{\rm rs}$  is a measure of upwelling radiance in a specific direction,<sup>1,7</sup> but  $b_b$  is a measure of photons scattered in all backward directions.<sup>24</sup> Depending on sensor solar geometry,  $r_{\rm rs}$  could include both forward-scattered and back-scattered photons. Therefore  $r_s$  depends on the angular redistribution of scattered photons. When  $r_{\rm rs}$  is simplified to a concise form such as Eq. (2), the angular dependence feature of  $r_{\rm rs}$  is transferred to parameter  $g.^{1,6,25}$ Since the redistribution of scattered photons is significantly different between molecular and particle scatterings, the g value that resulted from molecular scattering is expected to differ from that obtained with particle scattering, although both cases can have the same  $b_b/(a + b_b)$  ratios. This fact or feature, however, is lost by a model form such as in Eq. (3).

To remedy the above limitations, Morel and Gentili<sup>6</sup> and Morel et al.<sup>15</sup> developed a look-up table (LUT) for different solar zenith angles and sensor viewing angles and for different wavelengths and chlorophyll concentrations. This LUT, however, covers only a few wavelengths and chlorophyll concentrations. Because of the nonlinear nature of  $r_{\rm rs}$ with wavelength and chlorophyll concentration,<sup>6,26</sup> it is not clear how to interpolate or extrapolate the LUT for wavelengths or chlorophyll concentrations that are not included in the LUT. More importantly, the chlorophyll-based LUT was developed by use of empirical relationships that express water's optical properties (absorption, scattering) as functions of chlorophyll concentration.<sup>6,26</sup> For example, the absorption coefficient of gelbstoff at 440 nm  $[a_{\sigma}(440)]$  is fixed explicitly (20% of the absorption coefficient of chlorophyll at 440 nm<sup>6,26</sup>) or inexplicitly<sup>15</sup> as a function of chlorophyll concentration, as is particle scattering.<sup>6,15</sup> It is then difficult to apply the LUT to waters that do not follow these predefined exclusive case-1 relationships,<sup>27</sup> especially for waters in a coastal area.<sup>28</sup> Actually, in ocean color remote sensing it is not known whether the optical properties of a study area follow the statistically derived relationships before the values are derived. An  $r_{\rm rs}$  model, with the different scattering-distribution effects accounted for and applicable to more wavelengths and a wider range of waters with less restriction, is cer-

Table 1. Values Used in the HydroLight Simulations

| Variable  | Input  |  |
|---|--|--|
| $\begin{array}{l} \text{Solar zenith angle} \\ [C] \ (\text{mg m}^{-3}) \\ F \\ B_p \\ \lambda \ (\text{nm}) \end{array}$ | 30°<br>0.03, 0.1, 0.5, 1.0, 5.0, 10.0, 30.0<br>0.2, 0.8, 2.5<br>0.1, 0.3, 1.0<br>400–700 every 20 nm |  |

tainly desired for ocean color research and remotesensing applications.

Here we first illustrate numerically the effects of molecular and particle scatterings on the values of g. To overcome some of the limitations of the traditional model, we developed an innovative semianalytical  $r_{\rm rs}$  model. The model mimics closely the contributions of molecular and particle scatterings to  $r_{\rm rs}$  and accurately reproduces the reflectance spectra generated by Hydrolight. Also, as the model is based on absorption and backscattering properties instead of chlorophyll concentrations, it can be applied to a wider range of waters not limited to case-1 water, as long as absorption and scattering properties are provided.

# 2. HydroLight Simulations

Because of multiple scattering, it is difficult (if not impossible) to derive exact g values from the radiative transfer equation, unless the light field can be determined by single scattering.<sup>1,29</sup> As in earlier studies,<sup>6,13</sup> values of g were derived from numerically simulated  $r_{rs}$  for different values of a and  $b_b$ , by use of a widely accepted HydroLight numerical model<sup>18,30</sup> to compute a subsurface light field. As an example, results with the Sun positioned at 30° from zenith, a wind speed of 5 m/s and a sensor viewing at nadir were used to demonstrate g variations and subsequent analysis and modeling. Table 1 summarizes the properties and wavelengths used in the HydroLight calculations, where the absorption coefficients for pure water were taken from Pope and Fry,<sup>31</sup> pigment concentration ([C]) varies from 0.03 to 30.0 mg/m<sup>3</sup> to obtain a wide range of absorption and scattering coefficients, and the water column is assumed infinitely deep and homogeneous.

In the HydroLight simulations, bottom reflectance and inelastic scatterings (such as Raman scattering) are excluded as they are beyond the scope of this study. Their contributions to  $r_{\rm rs}$  are discussed by Sathyendranath *et al.*,<sup>32</sup> and by Lee *et al.*<sup>33,34</sup> The solar input and spectral bio-optical models used in the calculations are those provided in the HydroLight model, with adjustments made with regard to the generation of  $a_g(440)$  and  $b_p(550)$  (particle scattering coefficient at 550 nm). In the Hydrolight simulations,  $a_g(440)$  is modeled as  $a_g(440) = F a_{\phi}(440)$  $[a_{\phi}(440)$  is the absorption coefficient of phytoplankton pigments at 440 nm] with a default *F* value of 0.2 for all waters. In the calculations reported here, *F* values of 0.2, 0.8, and 2.5 were used to observe their effects on the values of g, since F is not a constant for both coastal and oceanic waters.<sup>28,35–37</sup>

As in many earlier studies,<sup>5,7,16,27,38</sup> water scattering is separated as scattering from water molecules and scattering from suspended particles (anything other than molecules), with a phase function for particle scattering from Mobley.<sup>18</sup> Further,  $b_p(550)$  is expressed as<sup>16,27</sup>

$$b_p(550) = B_p[C]^{0.62}, \qquad (4)$$

where  $B_p$  is a model parameter with a default value of 0.3 in HydroLight. In the calculations here,  $B_p$ values of 0.1, 0.3, and 1.0 were used to observe their effects on g. This  $B_p$  variation is based on the facts presented by Gordon and Morel<sup>16</sup> and by Loisel and Morel,<sup>39</sup> where the  $B_p$  values varied from less than 0.1 to more than 1.0 when  $b_p(550)$  is simply expressed as a function of [C]. This is not a surprise since particle scattering  $(b_p)$  includes all the scattering effects other than molecular scattering, which includes scattering by phytoplankton,<sup>16</sup> bacteria,<sup>40</sup> suspended sediments,<sup>16</sup> and bubbles.<sup>41</sup> Therefore a fixed  $B_p$ value in Eq. (4) is inadequate to describe the  $b_p$  variation of natural waters. Since we used a wide range of  $B_p$  values in this study, the input  $b_p$  is actually an independent variable not restricted by the case-1 assumptions.<sup>27</sup>

Note that the light field is actually determined by absorption and scattering properties;<sup>7</sup> the bio-optical models and the [C] values used in the HydroLight simulations merely to provide a wide range of optical properties.<sup>38</sup> When  $r_{\rm rs}$  is modeled as a function of absorption and scattering properties, how the absorption and scattering coefficients relate exactly to phytoplankton concentration is beyond the scope of this study, as long as the absorption and scattering coefficients range.

# 3. Values and Variations of g

From the calculated  $r_{rs}$  and the input *a* and  $b_b$  values, we easily derived values of g by using Eq. (2). As examples, Figs. 1(a) and 1(b) present the influence of different F and  $B_p$  values on the values of g, where [C] is set as 1.0 mg/m<sup>3</sup>. Clearly, for a given [C] value, different F and  $B_p$  values change the absorption and scattering properties of the water (as normally observed in the field<sup>28</sup>). Consequently gvalues could vary by as much as 30% for the same [C]. More variations are especially found in the bluegreen domain, where spectral bands are used to rewater properties from water color.<sup>16</sup> trieve Therefore it is necessary to be cautious when applying  $r_{\rm rs}$  models that have only a [C] value as a variable if fewer uncertainties are desired.

It is always interesting to know how existing models perform in the generation of  $r_{\rm rs}$  spectra for given spectra of a and  $b_b$ . For this purpose, Fig. 2 presents examples of  $r_{\rm rs}$  from HydroLight computations and  $r_{\rm rs}$  from two models. In Fig. 2(a) we used Eqs. (2)



Fig. 1. Variation of g spectra (nadir viewed) for different input parameters. In both (a) and (b)  $[C] = 1.0 \text{ mg/m}^3$ , in (a)  $B_p = 0.3$  and F varies, in (b) F = 0.2 and  $B_p$  varies.

and (3) to model  $r_{\rm rs}$  and in Fig. 2(b) we used the model of Jerome *et al.*,<sup>3</sup> where  $r_{\rm rs}$  is empirically modeled as

$$r_{\rm rs} = -0.00042 + 0.112 \frac{b_b}{a} - 0.0455 \left(\frac{b_b}{a}\right)^2$$
. (5)

In general, both models performed reasonably well for these sample  $r_{\rm rs}$  spectra. The  $r_{\rm rs}$  spectra obtained with Eqs. (2) and (3) is approximately 10–20% higher than Hydrolight  $r_{\rm rs}$  for the longer wavelengths, where particle scattering usually dominates. The  $r_{\rm rs}$  spectra obtained with Eq. (5), however, due to its empirical formulation, can result in significantly erroneous  $r_{\rm rs}$  values when  $b_b/a$  is small. The larger errors in the longer wavelengths could result in extra uncertainties in atmospheric properties if inaccurate  $r_{\rm rs}$  values are applied to processes for atmospheric correction.<sup>42</sup>

Figure 3 presents Hydrolight-derived g values of this study, which cover  $b_b/(a + b_b)$  up to 0.38 with varying fractions of gelbstoff absorption and various relative contributions of particle scattering. Also shown in Fig. 3 are the g values modeled by Eq. (3). As indicated in earlier studies,<sup>6,43</sup> g values generally range from 0.08 to 0.15 sr<sup>-1</sup> for an average particle phase function,<sup>18</sup> and generally follow a pattern described by Eq. (3). In contrast to Eq. (3), however, multiple g values were found for the same  $b_b/(a + b_b)$ 



Fig. 2. Nadir-viewed  $r_{\rm rs}$  from HydroLight compared with  $r_{\rm rs}$  from semianalytical models: (a)  $r_{\rm rs}$  is modeled by Eqs. (2) and (3) and (b)  $r_{\rm rs}$  is modeled by Eq. (5). In both (a) and (b)  $[C] = 1.0 \text{ mg/m}^3$ , F = 0.8,  $B_p$  varies from 0.1 (circles) and 0.3 (triangles down) to 1.0 (squares).

ratios. The scatter of a g value is more pronounced for cases with  $b_b/(a + b_b) < 0.1$ , and most oceanic waters fall within this range.<sup>44</sup>

Multiple *g* values are due mainly to the fact that *g* depends on the angular distribution of the water volume scattering function ( $\beta$ ).<sup>1,7</sup> Recall that water



Fig. 3. Traditional g [Eq. (2)] from HydroLight-simulated  $r_{\rm rs}$  (viewed at nadir). As expected from theory, multiple g values exist for the same  $b_b/(a + b_b)$  ratios. The solid line represents values from Eq. (3).

scattering is separated into scatterings by water molecules and scatterings by particles, resulting in a  $\beta$ of the water medium as  $\beta = \beta_w + \beta_p \cdot ^{6,18} \quad \beta_w$  (volume scattering function of water molecules) is a constant background,  $^{18,45}$  but  $\beta_{\rm p}$  (volume scattering function of particles) increases with concentrations of particles. Since the angular distribution is significantly different between  $\beta_w$  and  $\beta_p$ ,<sup>18</sup> the angular distribution of  $\beta$  varies with the amount of particles present in the water (see Fig.1 in Morel and Loisel<sup>46</sup>). For two cases, as an example, assume that they have the same  $b_b/(a + b_b)$  ratios. But, depending on the combination of  $\beta_w$  and  $\beta_p$ ,  $\beta$ of one case can be dominated by  $\beta_w$  whereas  $\hat{\beta}$  of another case can be dominated by  $\beta_p$ , therefore resulting in different g values. Since  $r_{\rm rs}$  is described as a simple product of g and  $b_b/(a + b_b)$ , the existing models for  $r_{\rm rs}$  [such as Eqs. (2) and (3) or Eq. (5)] are apparently insufficient to cope with the change in angular distribution of  $\beta$  that resulted from the increase of  $\beta_p$ .

## 4. r<sub>rs</sub> Model with Separate g Parameters

Based on  $\beta = \beta_w + \beta_p$  and in an approach analogous to Eq. (2), we can rewrite Eq. (2) as follows to incorporate the  $\beta_p$ -introduced angular variation:

$$r_{\rm rs} = g_w \frac{b_{\rm bw}}{a+b_b} + g_p \frac{b_{\rm bp}}{a+b_b}.$$
 (6)

Here  $b_b = b_{bw} + b_{bp}$  and  $b_{bw}$  and  $b_{bp}$  are the backscattering coefficients for water molecules and suspended particles, respectively.  $g_w$  and  $g_p$  are two independent model parameters for molecular scattering and particle scattering, with molecule-particle interscatterings embedded implicitly into both terms.

Comparing Eq. (2) with Eq. (6) yields the expression for the traditional g [Eq. (3)]:

$$g = g_w \frac{b_{\rm bw}}{b_b} + g_p \frac{b_{\rm bp}}{b_b}.$$
 (7)

The traditional g value is now partitioned and weighted by a molecular contribution  $(b_{\rm bw})$  and a particle contribution  $(b_{\rm bp})$ , as Morel and Loisel<sup>46</sup> did when they described the influence of molecular scattering on the model parameters for the downwelling diffuse attenuation coefficient. The g value will approach that determined by molecular scattering  $(g_w)$ when particle scattering is negligible (oceanic waters at blue wavelengths, for example), and will approach that determined by particle scattering when molecular scattering is negligible (sediment-abundant coastal waters, for example). Therefore, the g variation that resulted from the change in angular distribution of  $\beta$  is now considered, at least to first order.

The values and variations of the newly introduced model parameters  $(g_w \text{ and } g_p)$ , however, are not yet known. To determine their values and variations, the above HydroLight simulated data best serves the purpose.

An initial  $g_w$  value was derived by linear regression



Fig. 4. Calculated  $g_p$  values (open circles) with  $g_w$  set as the initial value of 0.1107 sr<sup>-1</sup>. Most of the  $g_p$  values are quite predictable with the values of  $b_{bp}/(a + b_b)$  (dotted curve), except a few points fall slightly out of the  $g_p$  versus  $b_{bp}/(a + b_b)$  pattern (see text for discussion).

analysis, which used values of  $b_{\rm bp}/b_b$  as the independent and values of g as the dependent [Eq. (7)]. The g versus  $b_{\rm bp}/b_b$  data came from Hydrolight simula-tions of  $[C] = 0.03 \text{ mg/m}^3$  with  $B_p = 0.1$ , and the intercept of 0.1107 sr<sup>-1</sup> of the linear regression (where  $b_{bp} = 0$ ) became the initial  $g_w$ . By applying this initial  $g_w$  (0.1107) into Eq. (7), we easily calculated values of  $g_p$ . Figure 4 presents these calculated  $g_p$  values versus values of  $b_{\rm bp}/(a + b_b)$ . Clearly, values of  $g_p$  are not a constant and generally increase with the ratio of  $b_{\rm bp}/(a + b_b)$  to account for the contributions that resulted from multiple scatterings [similar to g versus  $b_b/(a + b_b)$  shown in Fig. 3]. Compared with the relationship between g and  $b_b/$  $(a + b_b)$  shown in Fig. 3, however,  $g_p$  values follow a much tighter and predictable pattern with  $b_{\rm bp}/(a +$  $b_b$ ) (the dotted curve in Fig. 4), although some residual scatter points still exist. These scatters occur because the 0.1107 initial  $g_w$  value has practically no particle scattering. When particle scattering exists, so does molecule-particle interscattering. For such a case, we should expect the actual  $g_w$  value to be larger than the initial 0.1107 to include a portion of the interscatterings, unless a third term is introduced specifically for this interscattering contribution, as is done in atmospheric correction algorithms.<sup>47</sup>

To model  $r_{\rm rs}$  analytically as a function of absorption and backscattering coefficients, the  $g_p$  versus  $b_{\rm bp}/(a~+~b_b)$  relationship (Fig. 4) can be adequately described by use of

$$g_p = G_0 \left[ 1 - G_1 \exp\left( -G_2 \frac{b_{\rm bp}}{a + b_b} \right) \right], \qquad (8)$$

where  $G_0$ ,  $G_1$ , and  $G_2$  are constants for the specified light geometry and particle phase function. Since our purpose is to provide an  $r_{\rm rs}$  model that is consistent with theory and is accurate in the generation of  $r_{\rm rs}$  for given absorption and scattering properties, the



Fig. 5. g values (of nadir-viewed  $r_{\rm rs}$ ) from HydroLight compared with g values modeled by a combination of Eqs. (7) and (8).

combination of  $g_w$  and  $(G_0, G_1, G_2)$  that minimizes the  $r_{\rm rs}$  model error achieves this goal. Therefore, values of  $g_w$  and  $(G_0, G_1, G_2)$  were rederived by best fitting the HydroLight-derived g values with a combination of Eqs. (7) and (8), as was done in the earlier studies to derive values of model parameters.<sup>3,5,13</sup> The resulting values for nadir-viewed  $r_{\rm rs}$  are  $g_w = 0.113$  and  $(G_0, G_1, G_2) = (0.197, 0.636, 2.552)$ . As expected, the new  $g_w$  value is slightly larger than its initial value, since it also includes some of the contributions from molecule–particle interscatterings.

Figure 5 presents g values modeled from Eqs. (7) and (8) versus those calculated from HydroLight simulations. As expected, g values from the model match the g values from HydroLight excellently, with an average difference of 0.9% (1953 total points). As  $r_{\rm rs}$  is also a simple product of g and  $b_b/(a + b_b)$  [Eq. (2)], more accurate  $r_{\rm rs}$  values can now be obtained semianalytically. Note that, since there are multiple g values for the same  $b_b/(a + b_b)$  ratio (Fig. 3), a simple change in the values of  $g_0$  and  $g_1$  in Eq. (3) cannot provide a monotonic relationship between g and  $b_b/(a + b_b)$ . And, because of the existence of multiple g values for the same  $b_b/(a + b_b)$  ratio, dif-



Fig. 6. Same as Fig. 5 but g is for  $r_{\rm rs}$  viewed at 20° (subsurface) from nadir and 90° from the solar plane.

Table 2. Model Parameters for Sun at 30° and the Average Particle Phase Function

| Viewing Angle                                   | $g_w$          | $G_0, G_1, G_2$                            |
|---|----------------|--|
| Nadir 20° (0–) from nadir, 90° from solar plane | 0.113<br>0.111 | 0.197, 0.636, 2.552<br>0.189, 0.627, 3.204 |

ferent  $g_0$  and  $g_1$  values were derived from different g versus  $b_b/(a\,+\,b_b)$  data sets.  $^{5,43}$ 

So far only model results for nadir-viewed  $r_{\rm rs}$  have been presented. As an example, Fig. 6 presents HydroLight calculated and the analytical functions modeled g values for  $r_{\rm rs}$  values measured at  $20^\circ$ (subsurface) from nadir and 90° from the solar plane, because many field measurements are collected in such an orientation.<sup>21,48,49</sup> As shown for  $r_{\rm rs}$  at nadir, Eq. (3), which was developed for nadir-viewed  $r_{\rm rs}$ , cannot accurately model the g values of these simulations. Using Eqs. (7) and (8), HydroLight g is accurately reproduced (average difference is  $\sim$  1%), given a slightly different set of model values:  $g_w$  = 0.111 and  $(G_0, G_1, G_2) = (0.189, 0.627, 3.204)$ . Clearly, Eqs. (7) and (8) can be used to reproduce HydroLight-derived g values for different illumination and viewing geometries by varying the parameter values appropriately. Therefore the analytical  $r_{\rm rs}$  function [Eq. (6)] can be used in remote-sensing algorithms for efficient image processing without losing much accuracy in the generation of  $r_{\rm rs}$  spectra.

## 5. Conclusions

From results of numerical simulations it is found that the traditional simple model for parameter g [functions such as Eq. (3)] is insufficient to describe its variation. Basically, because of different angular distributions between molecular and particle scatterings, multiple g values exist for the same  $b_b/(a + b_b)$ value. The simple g model such as Eq. (3), however, will always refer to one g value for a  $b_b/(a + b_b)$  ratio. Further, when different portions of the g versus  $b_b/(a + b_b)$  data set were used for the derivation of  $g_0$  and  $g_1$ , different values were obtained.<sup>5,43</sup>

To overcome a shortfall of the traditional approach, an innovative  $r_{\rm rs}$  model has been developed. This model still describes  $r_{\rm rs}$  as a function of absorption and backscattering coefficients, but, instead of the traditional simple term, this model uses separate parameters to account explicitly for the distribution effects on  $r_{\rm rs}$  that result from molecular scattering and particle scattering. The form of the model is, in principle, consistent with the radiative transfer theory. With values of model parameters derived from HydroLight simulations, the model thus provides an explicit tool to better understand and quantify the contributions of molecular and particle scatterings to remote-sensing reflectance, and to cope easily with the multiple g values that exist for the same  $b_b/a$ ratio.

The new  $r_{\rm rs}$  model [Eq. (6)] has a maximum error of  $\sim 3.5\%$  and an average error of  $\sim 0.9\%$  for nadirviewed  $r_{\rm rs}$  in this study. Therefore, for given optical properties, the new model provides  $r_{\rm rs}$  spectra that closely match theoretical values. This is an important and useful improvement for reaching the desired goal of remotely estimating chlorophyll concentration to within 35%.<sup>50</sup> And, as  $r_{\rm rs}$  is expressed as a simple analytical function of absorption and backscattering coefficients, it can be applied to ocean optics studies and remote-sensing algorithms to calculate  $r_{\rm rs}$  spectrum efficiently.

Table 2 lists the model parameter values  $(g_w, G_0,$  $G_1$ , and  $G_2$ ) for two viewing geometries and one particle phase function. Parameter tables for various light geometries and particle phase functions can be developed as well, which can then be used in modeling of remote-sensing reflectance and ocean color algorithms over a wide range of waters. As the values of these model parameters  $(G_0, G_1, \text{ and } G_2)$  more or less vary with the shape of the particle phase function, the challenge that follows, especially in ocean color remote sensing, is to know how to assign proper and accurate particle phase functions to different waters. Extensive measurements and classification of biogeochemical provinces<sup>51,52</sup> can provide clues for the assignment. Also, since it is difficult to know precisely the actual particle phase function from remote sensing, the effects of an incorrect phase function assignment to the retrieval of absorption and scattering properties from remote sensing will be analyzed in the future. Nevertheless, the new  $r_{rs}$ model developed here provides more insight and understanding with regard to the contributions of molecular and particle scatterings to  $r_{\rm rs}$ .

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